

MATH 1314 – COLLEGE ALGEBRA SECTION 2.4 COMPLEX NUMBERS

- Imaginary Numbers – based on the imaginary unit i , where $i = \sqrt{-1}$. Note: $i^2 =$
- Complex numbers – numbers that can be written in the form $a + bi$, where a and b are real numbers and $i = \sqrt{-1}$. a is the real part, and b is the imaginary part.
- Simplifying Imaginary numbers – follow the rules of exponents.
Ex: Simplify (a) $(4i)^2$ (b) $\sqrt{-36}$

- NOTE: If a and b are both negative, then $\sqrt{ab} \neq \sqrt{a}\sqrt{b}$.
Ex: Simplify $\sqrt{-25}\sqrt{-4}$

- Two complex numbers are equal if their real parts are equal and their imaginary parts are equal.
 $a + bi = c + di$ if $a = c$ and $b = d$.

Ex: Find the values of x and y if $x + (x + y)i = 3 + 8i$.

Ex: Simplify $(5 - 2i) + (-3 + 9i)$.

Ex: Simplify (a) $(3 + \sqrt{-36})(7 - \sqrt{-16})$

(b) $(5 + \sqrt{-16})(5 - \sqrt{-16})$

- The complex numbers $a + bi$ and $a - bi$ are _____ of each other.
In general, $(a + bi)(a - bi) =$

Ex: Divide and write in $a + bi$ form: $\frac{3}{2-i}$

Ex: Simplify: $\frac{3 + \sqrt{-25}}{2 - \sqrt{-1}}$

■ Powers of i :

Ex: Simplify

(a) i^{43}

(b) i^{365}

(c) i^{440}

(d) i^{29}

(e) i^{18}

(f) $\frac{3}{i^5}$